

*TESTING OF HYPOTHESIS OF LATENT
STRUCTURE MODEL'S PARAMETERS: A
SIMULATION STUDY*

*A dissertation submitted for the Degree
of*

Doctor of Philosophy

by

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DEDICATION

*I dedicate this to my beloved father Shamshad Ahmed (Late)
and to my dearest Mother & family.*

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CERTIFICATE

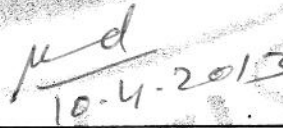
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